

EJERCICIO 2 Un transformador trifásico conectado en D-Y de 100 kVA, 15.000/380 V, 50 Hz, sometido a los ensayos de vacío y cortocircuito, proporciona los siguientes resultados:

Ensayo de vacío:  $P_0 = 1.200$  W,  $I_0 = 12$  A,  $U_0 = 380$  V.

Ensayo de cortocircuito:  $P_{cc} = 800$  W,  $I_{cc} = 3$  A,  $U_{cc} = 400$  V.

Determinar:

1.- Circuito equivalente referido al lado de AT y referido al lado de BT.

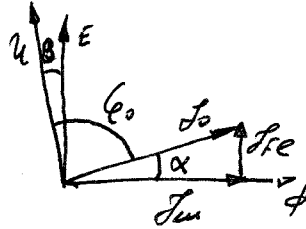
2.- La tensión en el secundario del transformador cuando la carga toma la corriente de régimen con  $\cos \phi = 0,8$  capacitivo. Dibujar el diagrama vectorial correspondiente.

$$1) S_m = \sqrt{3} U_{in} \cdot I_{in} \Rightarrow I_{in} = \frac{S_m}{\sqrt{3} \cdot U_{in}} = \frac{100.000}{\sqrt{3} \cdot 15.000} = 3,849 \text{ A}$$

$$I_{inf} = \frac{3,849}{\sqrt{3}} = 2,22 \text{ A}$$

$$P_0 = \sqrt{3} U_0 I_0 \cos \phi_0 \Rightarrow \cos \phi_0 = \frac{P_0}{\sqrt{3} U_0 I_0} = \frac{1.200}{\sqrt{3} \cdot 380 \cdot 12} = 0,1519 \Rightarrow \phi_0 = 81,26^\circ$$

$$\sin \phi_0 = 0,9884$$



$$P_{fe} = P_{f_0} = R_{fe} \cdot I_{fe}^2 = R_{fe} \left( \frac{U_{f_0}}{R_{fe}} \right)^2 = \frac{U_{f_0}^2}{R_{fe}}$$

$$\left( R_{fe} \right)_{BT} = \frac{U_{f_0}^2}{P_{f_0}} = \frac{\left( \frac{380}{\sqrt{3}} \right)^2}{1.200} = 120,33 \Omega$$

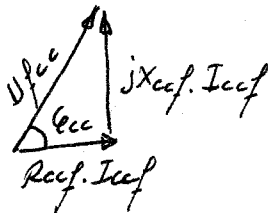
$$BT - \Delta \Rightarrow U_{f_0} = \frac{U_0}{\sqrt{3}} ; I_{0f} = I_0$$

$$I_{mf} = I_0 \sin \phi_0 = 12 \times 0,9884 = 11,84 \text{ A}$$

$$\left( X_{mf} \right)_{BT} = \frac{U_{f_0}}{I_{mf}} = \frac{\left( \frac{380}{\sqrt{3}} \right)}{11,86} = 18,50 \Omega$$

$$P_{cc} = \sqrt{3} U_{cc} I_{cc} \cos \phi_{cc} \Rightarrow \cos \phi_{cc} = \frac{P_{cc}}{\sqrt{3} U_{cc} I_{cc}} = \frac{800}{\sqrt{3} \cdot 400 \cdot 3} = 0,3849 \Rightarrow \phi_{cc} = 67,36^\circ$$

$$\sin \phi_{cc} = 0,9229$$



$$R_{ccf} \cdot I_{ccf} = U_{ccf} \cos \phi_{cc} \Rightarrow R_{ccf} = \frac{U_{ccf} \cos \phi_{cc}}{I_{ccf}}$$

$$X_{ccf} \cdot I_{ccf} = U_{ccf} \sin \phi_{cc} \Rightarrow X_{ccf} = \frac{U_{ccf} \sin \phi_{cc}}{I_{ccf}}$$

$$AT \rightarrow \Delta \Rightarrow U_{ccf} = U_{cc} ; I_{ccf} = \frac{I_{cc}}{\sqrt{3}}$$

$$\left( R_{ccf} \right)_{AT} = \frac{400 \times 0,3849}{\frac{3}{\sqrt{3}}} = 88,89 \Omega$$

$$\left( X_{ccf} \right)_{AT} = \frac{400 \times 0,9229}{\frac{3}{\sqrt{3}}} = 213,13 \Omega$$

$$r_b = \frac{U_{f_{AT}}}{U_{f_{BT}}} = \frac{15.000}{\frac{380}{\sqrt{3}}} = 68,3 \%$$

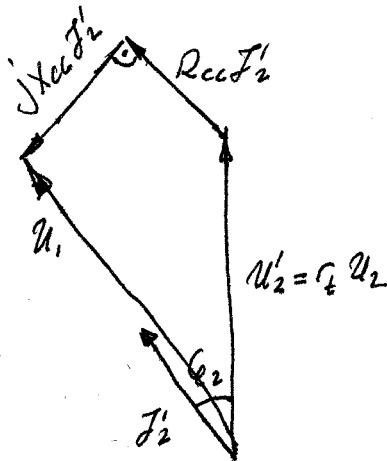
$$R_{\text{ref}_{AT}} = R_{\text{ref}_{BT}} \cdot r_t^2 = 120,33 \times 68,3\%{}^2 = \boxed{56,248 \Omega}$$

$$X_{\text{mf}_{AT}} = X_{\text{mf}_{BT}} \cdot r_t^2 = 18,50 \times 68,3\%{}^2 = \boxed{86,477 \Omega}$$

$$R_{\text{ccf}_{BT}} = \frac{R_{\text{cc}_{AT}}}{r_t^2} = \frac{88,89}{68,3\%{}^2} = \boxed{19 \times 10^{-3} \Omega}$$

$$X_{\text{ccf}_{BT}} = \frac{X_{\text{cc}_{AT}}}{r_t^2} = \frac{213,13}{68,3\%{}^2} = \boxed{45,60 \times 10^{-3} \Omega}$$

$$2) \quad AT \Rightarrow \Delta \Rightarrow I_{\text{inf}} = \frac{I_{\text{in}}}{\sqrt{3}} = \frac{3,849}{\sqrt{3}} = 2,22 \text{ A.}$$



$$U_{1f} = U'_{2f} + R_{\text{ccf}} I'_{2f} \cos \epsilon_2 - X_{\text{ccf}} I'_{2f} \sin \epsilon_2$$

$$U'_{2f} = U_{1f} - R_{\text{ccf}} I'_{2f} \cos \epsilon_2 + X_{\text{ccf}} I'_{2f} \sin \epsilon_2$$

$$U'_{2f} = 15.000 - 88,89 \times 2,22 \times 0,8 + 213,13 \times 2,22 \times 0,6 = 15.126 \text{ V}$$

$$U_{2f} = \frac{U'_{2f}}{r_t} = \frac{15.126}{68,3\%} = 221,24 \text{ V.}$$

$$BT \Rightarrow \lambda \Rightarrow U_{2f} = \frac{U_2}{r_t} \Rightarrow U_2 = r_t \cdot U_{2f} = 68,3\% \times 221,24 = \boxed{383,19 \text{ V}}$$

$$383,19 > 380 \Rightarrow \text{F. Ferranti}$$